

CMPU-224 Lab3 Practice

Spring 2025

1. You are given the following 6-bit two's-complement number.

100110

(a) What is the decimal value of this number?

-26

$$\begin{array}{r}
 -32 \ 16 \ 8 \ 4 \ 2 \ 1 \\
 1 \ 0 \ 0 \ 1 \ 1 \ 0 \\
 -32 + 6 = -26
 \end{array}$$

OR Take the Two's comp. To get magnitude

$$\begin{array}{r}
 011001 \\
 + \quad \quad 1 \\
 \hline
 011010 \\
 16 + 8 + 2 = 26
 \end{array}$$

(b) What is representation of that number as a 10-bit two's-complement number? Give your answer as in hexadecimal.

0x3C6

SIGN extend To 10 Bits

$$\begin{array}{cccccccccc}
 1 & 1 & 1 & 1 & 1 & 0 & 0 & 1 & 1 & 0
 \end{array}$$

2. You are given the following 6-bit two's-complement number.

001100

(a) What is the decimal value of this number?

12

(b) What is representation of that number as a 10-bit two's-complement number? Give your answer as in hexadecimal.

0x00C

Zero extend To 10-bits

$$\begin{array}{cccccccccc}
 0 & 0 & 0 & 0 & 0 & 0 & 1 & 1 & 0 & 0
 \end{array}$$

3. For this question, assume all the numbers are internally represented as 6-bit two's complement binary numbers.

(a) What is the decimal value of $30 + 12$?

-22

$$\begin{array}{r}
 -32 \ 16 \ 8 \ 4 \ 2 \ 1 \\
 42 \Rightarrow 101010 \\
 -32 + 10 = -22
 \end{array}$$

(b) What is the decimal value of $-22 + -22$?

20

$$\begin{array}{r}
 -64 \ 32 \ 16 \ 8 \ 4 \ 2 \ 1 \\
 -44 \Rightarrow 1010100 \Rightarrow 010100 \\
 \uparrow \\
 \text{DISCARD}
 \end{array}$$

(c) What is the decimal value of $-20 \gg 3$?

-3

$$\begin{array}{l}
 \boxed{-\frac{20}{8} \Rightarrow -2.5 \text{ (Round Down)}} \quad \text{OR} \\
 -20 \Rightarrow \begin{array}{r} -32 \ 16 \ 8 \ 4 \ 2 \ 1 \\ 1 \ 0 \ 1 \ 0 \ 1 \ 0 \end{array} \Rightarrow \text{shift } 3 \Rightarrow 11101 \Rightarrow -3
 \end{array}$$

4. Consider a 10-bit floating point representation called "Tiny Float".

The bits are arranged as follows:

Bit 9: Sign bit (S)

Bits 8–5: Exponent (E) $Bias = 2^{4-1} - 1 = 7$

Bits 4–0: Fraction (F)

Convert the decimal number -13.5 into the 10-bit Tiny Float representation.

(a) Convert the number to fixed-point binary.

$$13.5 = 1101.1$$

(b) Normalize the binary number (show the value in scientific notation like $1.xxxx \times 2^y$).

$$1.1011 \times 2^3$$

(c) Determine the values for the Sign bit, Exponent bits, and Significand bits.

$$\begin{aligned} S &= 1 \\ \text{Exp} &= 10 \quad (3+7) \Rightarrow 1010 \\ \text{frac} &= 10110 \quad (5\text{-bits}) \end{aligned}$$

(d) Write the final 10-bit binary representation.

Sign	Exponent	Significand
1	1010	10110

5. Consider the following Tiny Float represented in binary:

00101 10100

(a) Identify the sign, the biased exponent value (in decimal), and the stored fractional part.

$$\begin{aligned} s &= 0 \\ \text{exp} &= 0101 \\ \text{frac} &= 10100 \end{aligned}$$

(b) Calculate the actual exponent (unbiased) in decimal.

$$5 - 7 = -2$$

(c) Write the number in binary scientific notation (restoring the implicit leading 1).

$$1.10100 \times 2^{-2} \Rightarrow .01101$$

(d) Convert the result to a standard decimal number.

$$\begin{array}{r} .25 \\ .125 \\ .03125 \\ \hline 0.40625 \end{array}$$

$$\begin{array}{cccccc} .5 & .25 & .125 & .0625 & .03125 \\ 0 & 1 & 1 & 0 & 1 \end{array}$$